

Atmospheric Phenomena for Wind Energy

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October 18, 2022 TWIND short course



Who am I?

- Assistant professor in the Wind Energy Section at TU Delft
- BSc, MSc and PhD from KU Leuven, Postdoc at NREL (Boulder, CO, US)









What is my research background?

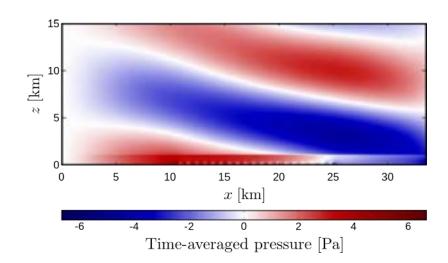
• Wind farm aerodynamics How does the wind flow in, above and around a wind farm?

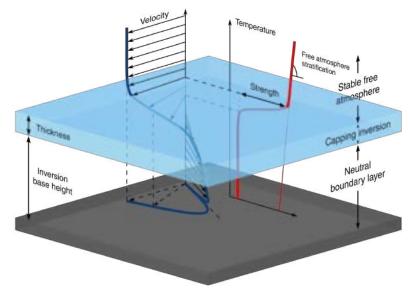
Topics include

- Global blockage effect
- Self-induced gravity waves
- Wind-farm wakes
- Boundary-layer meteorology
 How does the atmospheric boundary layer affect wind energy?

Topics include

- Atmospheric stability
- Capping inversion
- Low-level jets







What do you know about atmospheric phenomena for wind energy?





What would you like to learn today?

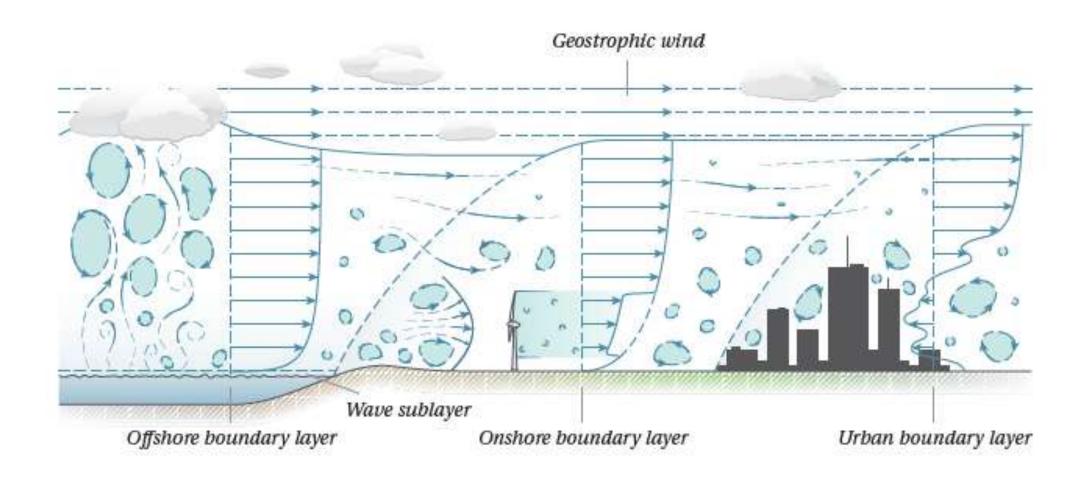




Atmospheric science: Why bother?



1) In wind energy, the inflow wind is the "fuel"



Source: Bos (2017)

2) Wind conditions drive design, operation and maintenance



Typhoon resistant wind turbines in the Akita Noshiro Offshore Wind Farm

3) Large wind farms interact with the atmosphere



Objectives of this lecture

- Give a brief introduction to atmospheric sciences for wind energy
- Explain some of the basic and widely used concepts in wind energy
- Provide relevant reference material for future study of wind energy meteorology
- Discuss any atmospheric science topics that are of interest to you



Outline

Motivation and objectives

Overview of relevant reference material

Part 1: General meteorology

Part 2: Boundary-layer meteorology

Part 3: Wind power meteorology

Take-home messages



Not covered today (at least not in detail)

- Mesoscale weather phenomena (frontal systems, thunderstorms, hurricanes, monsoons, etc.)
- Complex terrain (flow speed up, valley winds, fall winds, etc.)
- Forest and urban canopy flow
- Humidity, clouds, precipitaton
- Air-sea interaction
- Wind farm atmospheric boundary layer interaction
- Modelling and measuring techniques
- Climate change



Prior knowledge

- Calculus
- Thermodynamics
- Fluid mechanics
- Basics of wind energy
- A notion of turbulence



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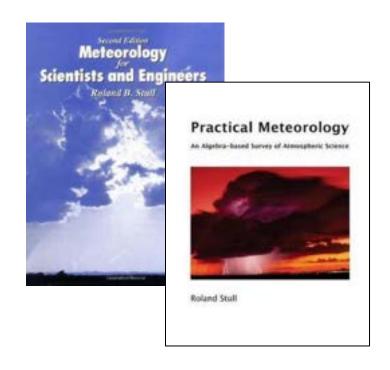
Reference material *Meteorology*

Stull – Practical Meteorology (2017)

successor of Meteorology for Scientists and Engineers

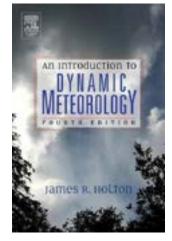
Available as e-book:

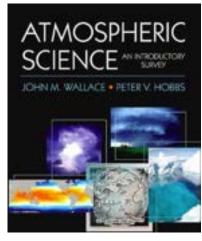
www.eos.ubc.ca/books/Practical Meteorology



Holton – An introduction to dynamic meteorology (1992)

Wallace & Hobbs – Atmospheric Science (2006)







Reference material Boundary-layer meteorology

Stull – An introduction to boundary layer meteorology (1988)

Garratt – The atmospheric boundary layer (1992)

Kaimal & Finnigan – Atmospheric boundary layer flows (1994)

Wyngaard – Turbulence in the atmosphere (2010)

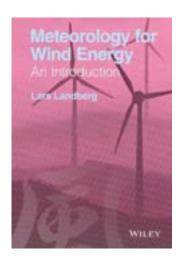


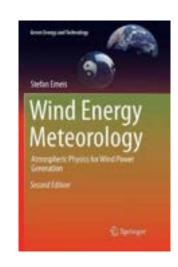


Reference material Wind energy meteorology

Landberg – Meteorology for wind energy (2016)

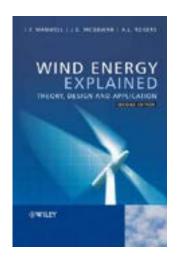
Emeis – Wind energy meteorology (2018)

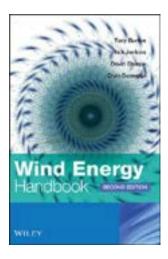




Dedicated chapters in wind energy textbooks: Manwell et al. – Wind energy explained (2009)

Burton et al. – Wind energy handbook (2018)







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Part 1: General meteorology

- What is wind?
- Why does the wind blow?
- Scales of atmospheric motion

Part 2: Boundary-layer meteorology

Part 3: Wind power meteorology

Take-home messages



What is wind?





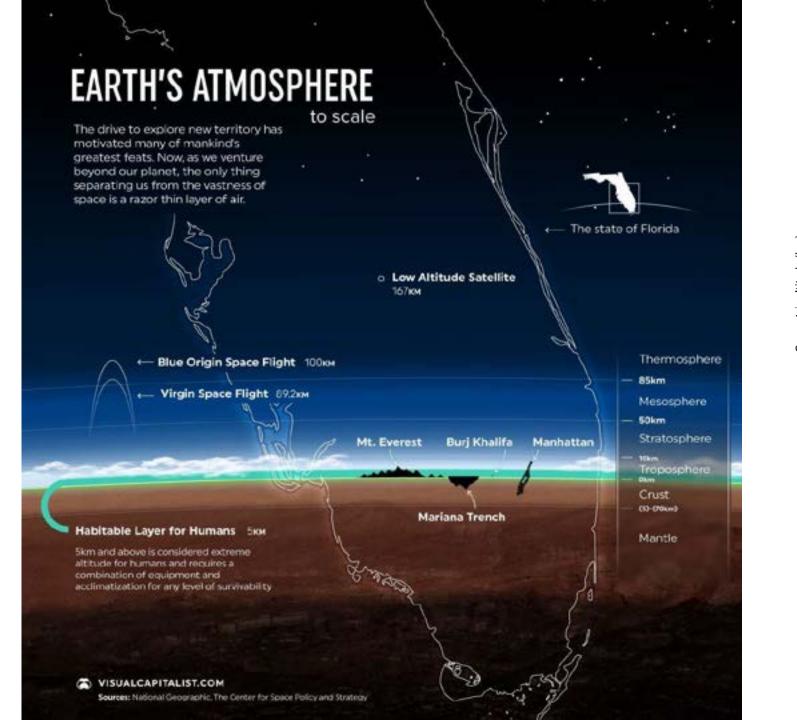
Image: NASA/NOAA/GSFC/Suomi NPP/VIIRS/Norman Kuring

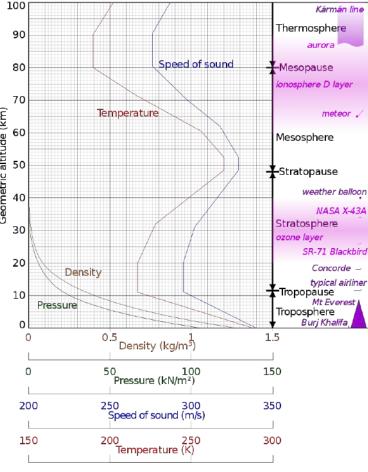


SMOOTH EARTH: If shrunk to a few inches across, Earth would feel as smooth as a billiard-hall cue ball.

7:02 PM · Apr 22, 2016 · TweetDeck

590 Retweets 9 Quote Tweets 2,356 Likes



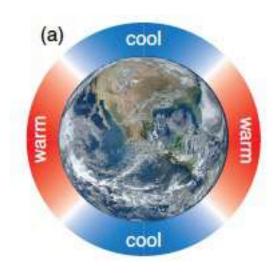


1962 US Standard Atmosphere graph of geometric altitude against air density, pressure, the speed of sound and temperature (source: Wikipedia)

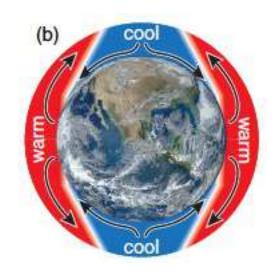
Why does the wind blow?



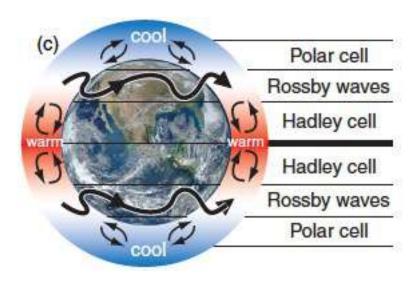
The origin of wind



Radiative imbalance creates warm tropics and cold poles



Differential heating powers a global atmospheric convection system



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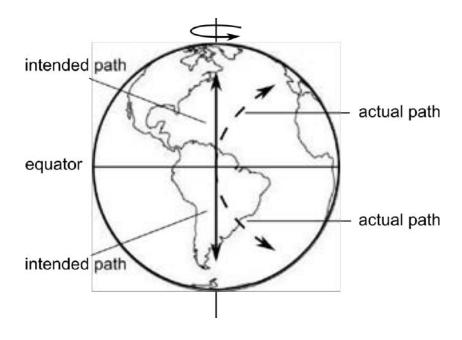
The rotation of the Earth leads to three circulation bands in each hemisphere

Source: Stull (2016)

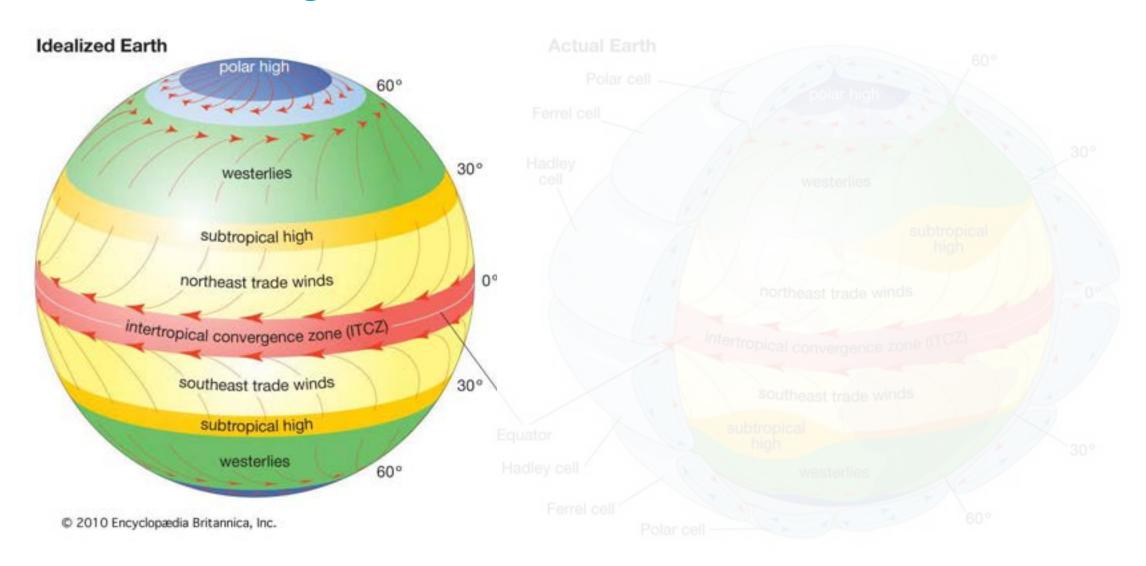
Intermezzo: Coriolis effect

- Due to Earth's rotation
- Motions are deflected to the right (northern hemisphere)
- Coriolis forces scale linear with wind speed
- Coriolis force is perpendicular to the velocity

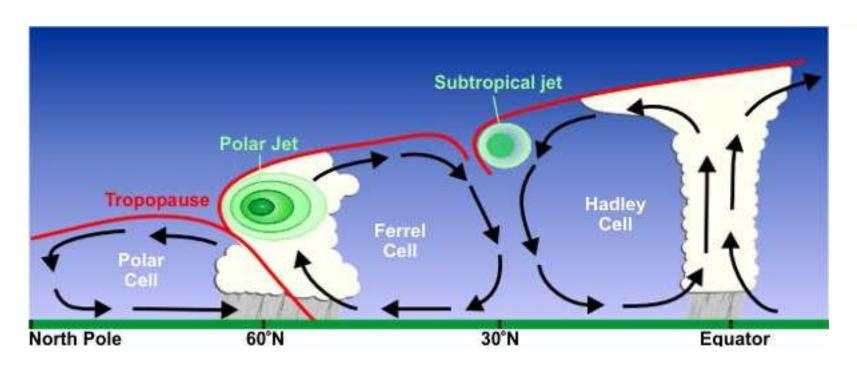
$$F_C = -2\rho\Omega \times u$$

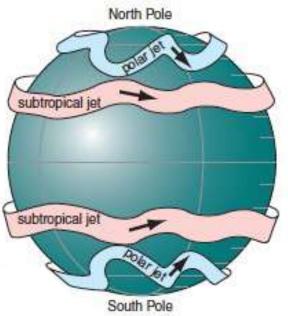


Three-band global circulation



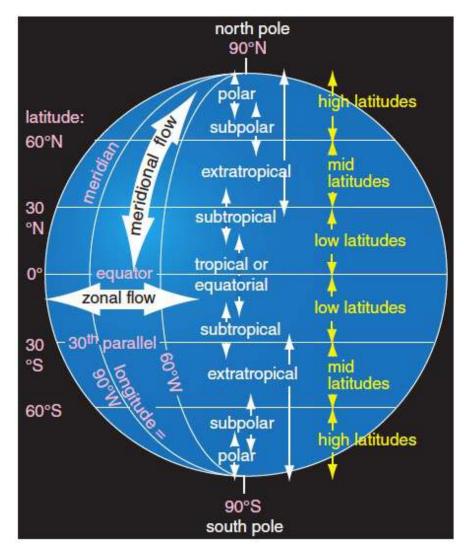
Jet streams

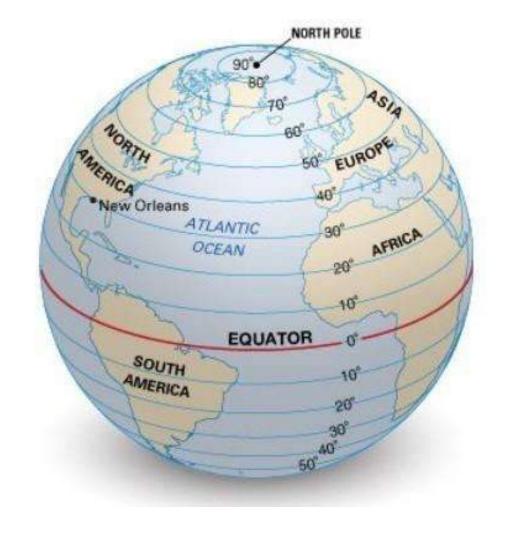




Source: Stull (2016)

Some key terms





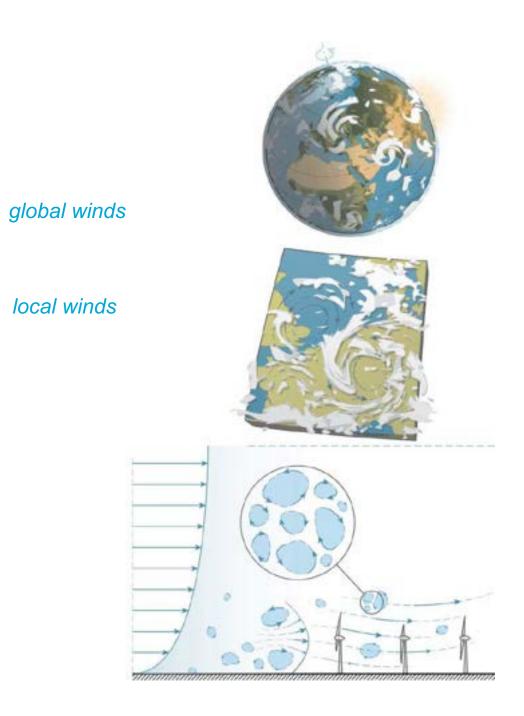
Source: Stull (2016)

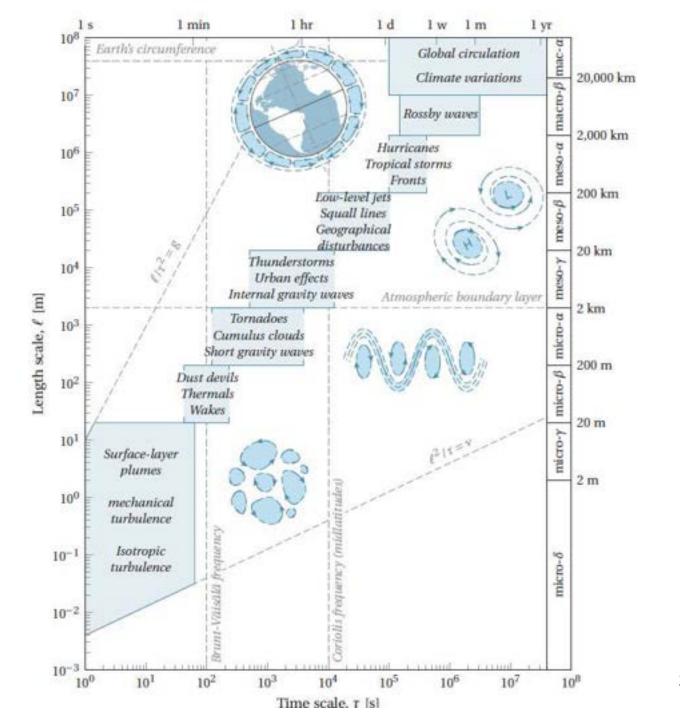
Scales of atmospheric motion



Horizontal Size 40,000 km 4,000 km	Scale		
	Designation		Name
40,000 km	macro α	planetary scale	
4,000 km - 700 km -	macro β	synoptic scale*	
300 km	meso α	mesoscale**	
30 km	meso β		
***************************************	meso γ		
3 km -	micro α	microscale***	boundary-layer turbulence
300 m – 30 m –	micro β		surface-layer turbulence
3 m	micro γ		inertial subrange turbulence
300 mm	micro δ		
30 mm		E	E fine-scale turbulence
3 mm -		dissination subvence	
0.3 µm -	viscous	dissipation subrange	
0.003 μm _ 0	molecular	mean-free path between molec.	
		molecule sizes	

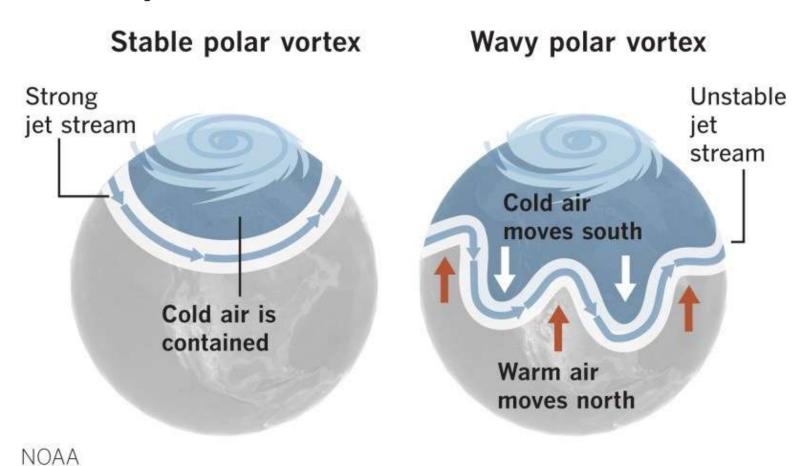
Source: Stull (2016)



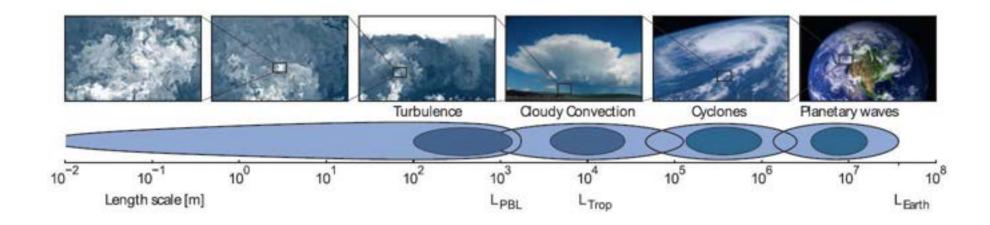


Example of planetary scale motions

How a polar vortex works



Multi-scale nature of atmospheric motions



Source: Schalkwijk et al. (2015)

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"The physics-based approach"

- The atmospheric boundary layer
- Vertical structure of the lower troposphere (free atmosphere, surface layer, Ekman layer)
- Atmospheric stability
- Selected topics of interest

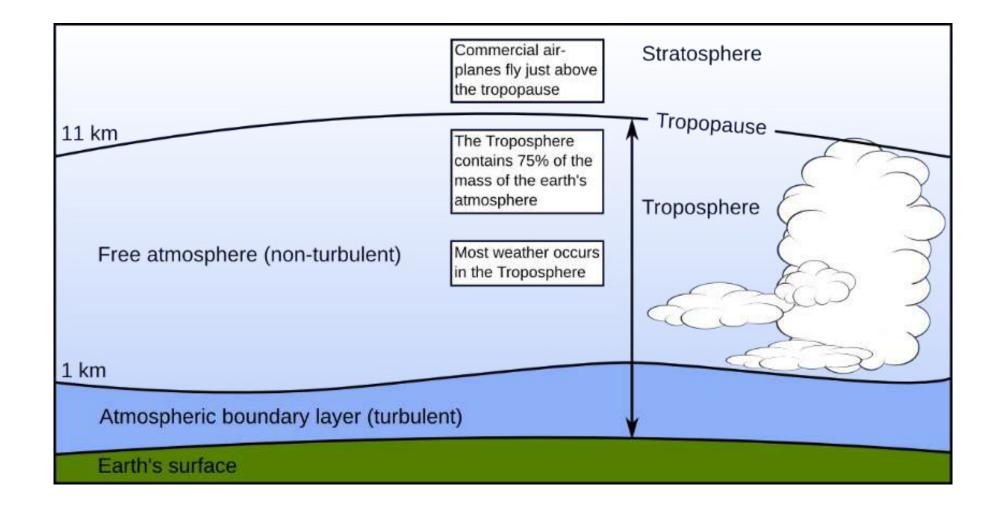
Part 3: Wind power meteorology

Take-home messages



Atmospheric Boundary Layer (ABL)

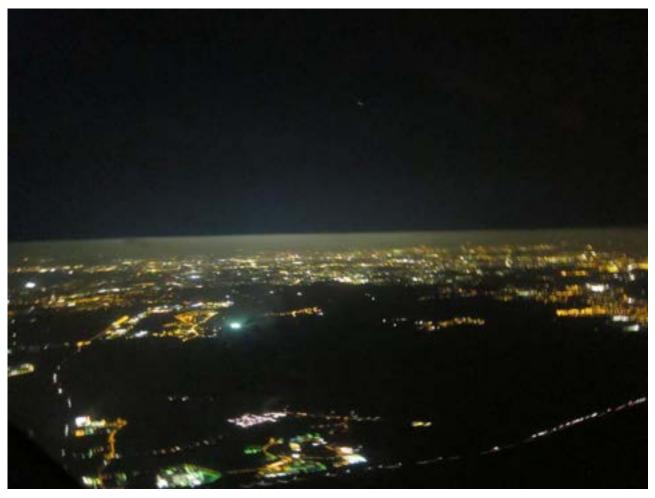
also called the planetary boundary layer (PBL)



"... that part of the troposphere that is directly influenced by the presence of the earth's surface, and responds to surface forcings with a timescale of about an hour or less."

Stull (1988)

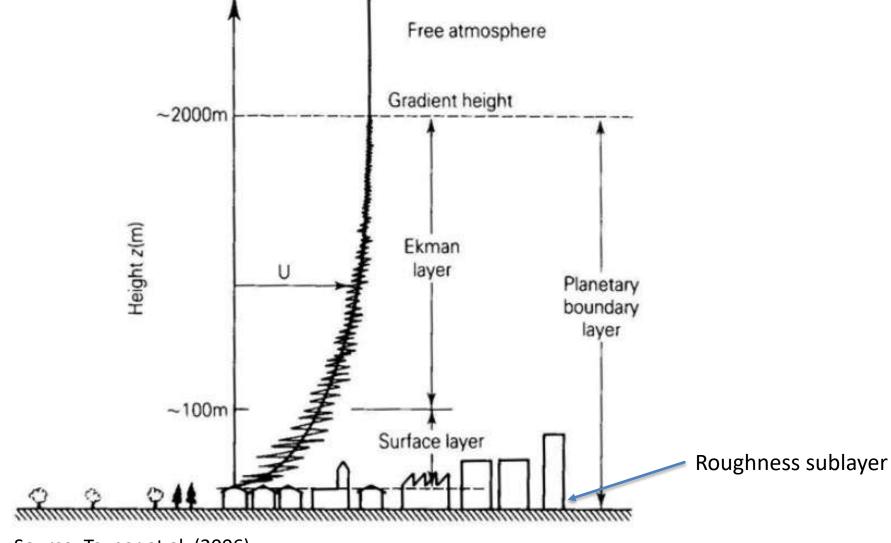
Atmospheric Boundary Layer (ABL)



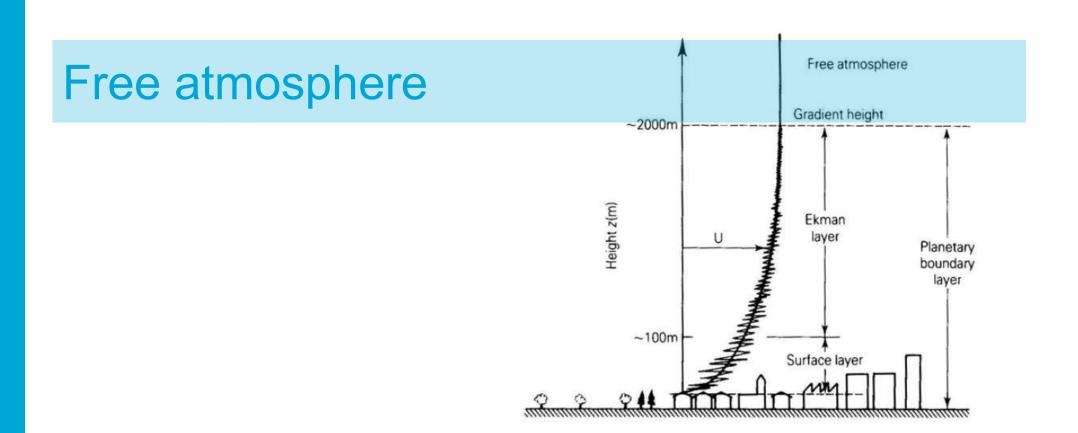
Planetary boundary layer over Berlin at night. Light pollution is easily scattered off of aerosols (suspended small particles) below the planetary boundary layer, but not so easily scattered in the clean air above.

Photo by Ralf Steikert, http://userpage.fu-berlin.de/~kyba/images/night_boundary_layer.html

Vertical structure of the lower troposphere



Source: Tavner et al. (2006)

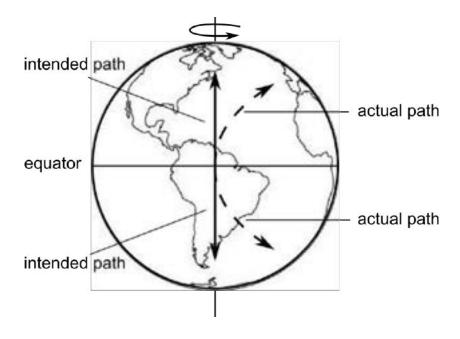




Intermezzo: Coriolis effect

- Due to Earth's rotation
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- Coriolis force is perpendicular to the velocity

$$F_C = -2\rho\Omega \times u$$



Geostrophic balance

Balance between pressure gradient and Coriolis force (horizontally homogeneous, no friction, steady state)

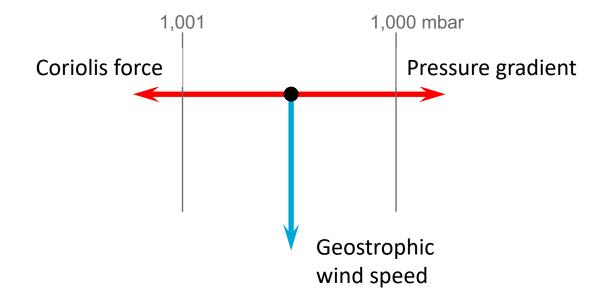
$$0 = -\frac{1}{\rho} \frac{\partial P}{\partial x} + f_c V_g$$
$$0 = -\frac{1}{\rho} \frac{\partial P}{\partial y} - f_c U_g$$

with Coriolis parameter $\,f_c=2\Omega\sin\phi\,$

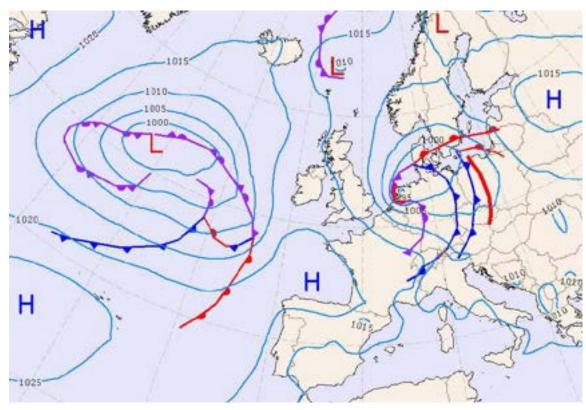
Geostrophic wind speed:

$$U_g = -\frac{1}{\rho f_c} \frac{\partial P}{\partial y}, \quad V_g = +\frac{1}{\rho f_c} \frac{\partial P}{\partial x}$$

Wind parallel to isobars



Geostrophic wind



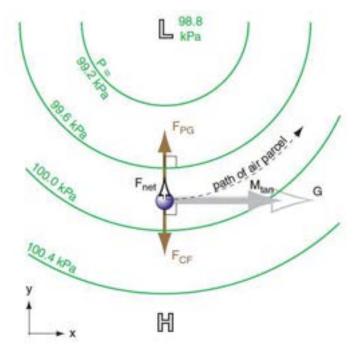
Isobars during a storm on 25 July 2015 (KNMI / WOW-NL)

Gradient winds around L or H

Balance between pressure gradient, Coriolis force and centrifugal force

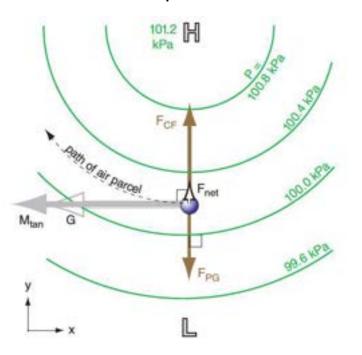
Low pressure system (cyclone)

Counterclockwise rotation in northern hemisphere



High pressure system (anticyclone)

Clockwise rotation in northern hemisphere



Source: Stull (2016)

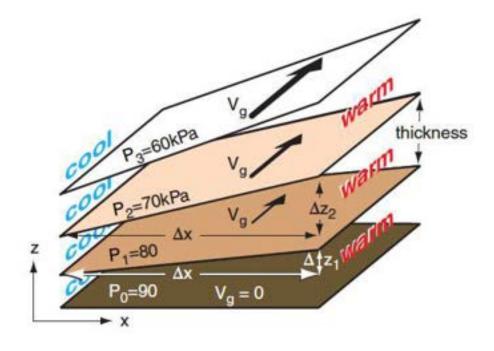
Thermal wind effect

Horizontal temperature gradients cause changes of the geostrophic wind with height

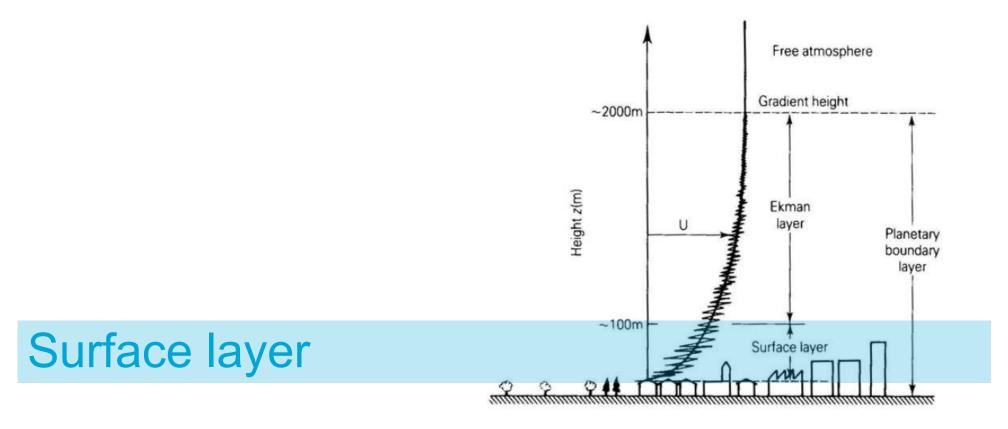
$$\frac{\partial U_g}{\partial z} \approx -\frac{g}{f_c T} \frac{\partial T}{\partial y}$$
$$\frac{\partial V_g}{\partial z} \approx +\frac{g}{f_c T} \frac{\partial T}{\partial x}$$

Barotropic conditions: U_g , $V_g = cst$

Baroclinic conditions: U_g , $V_g = f(z)$



Source: Stull (2016)







Logarithmic wind profile

Wind stress at the ground $au_0=
ho u_*^2$ with u_* defined as the friction velocity

Assume constant-stress layer, so $\tau=\rho u_*^2=\rho v_t \frac{\partial u}{\partial z}$ throughout the surface layer, with v_t an eddy-viscosity

Mixing length assumption (Prandtl) yields $\nu_t=\kappa u_*z$ with $\kappa=0.4$ the von Kármán constant

Hence,

$$\frac{\partial u}{\partial z} = \frac{u_*}{\kappa z} \quad \Rightarrow \quad u(z) = \frac{u_*}{\kappa} \ln(z/z_0)$$

with z_0 the surface roughness length, dependent on the surface coverage

Alternative: Power law

Empirical description of the vertical wind profile:

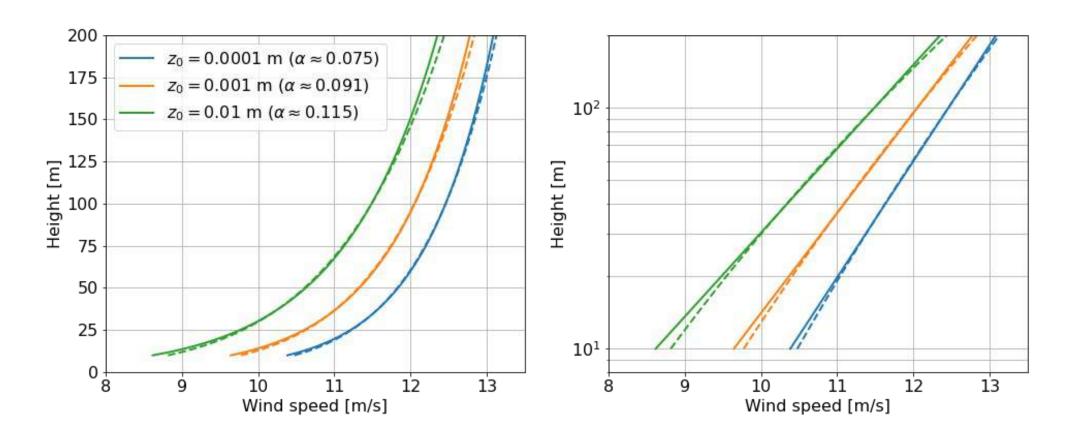
$$u(z) = u(z_{\mathrm{ref}}) \left(\frac{z}{z_{\mathrm{ref}}}\right)^{\alpha}$$

with α the shear exponent

Typical Roughness Lengths

Type of terrain	$z_0(m)$	α
Mud Flats, Ice	10 ⁻⁵ to 3x10 ⁻⁵	
Calm Sea	2x10 ⁻⁴ to 3x10 ⁻⁴	
Sand	2x10 ⁻⁴ to 10 ⁻³	0.01
Mown Grass	0.001 to 0.01	
Low Grass	0.01 to 0.04	0.13
Fallow Field	0.02 to 0.03	
High Grass	0.04 to 0.1	0.19
Forest and Woodland	0.1 to 1	
Built up area, Suburb	1 to 2	0.32
City	1 to 4	

Vertical wind profile



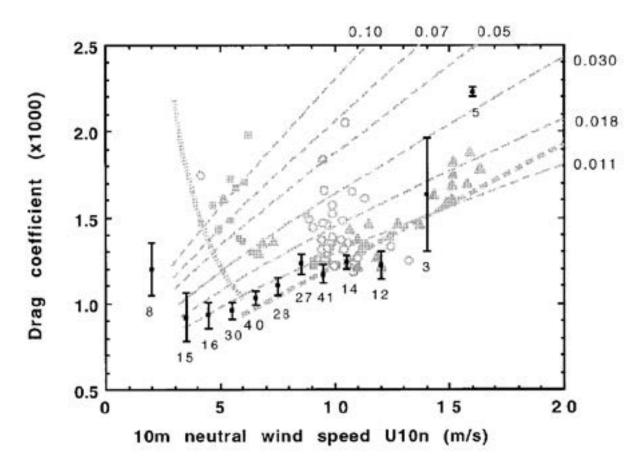
Full lines: Logarithmic profile Dashed lines: Power profiles

Offshore surface roughness

$$C_{D10n} = \frac{u_*^2}{U_{10}^2} = \frac{\kappa^2}{[\ln(10 \, m/z_0)]^2}$$

At sea, z₀ depends on

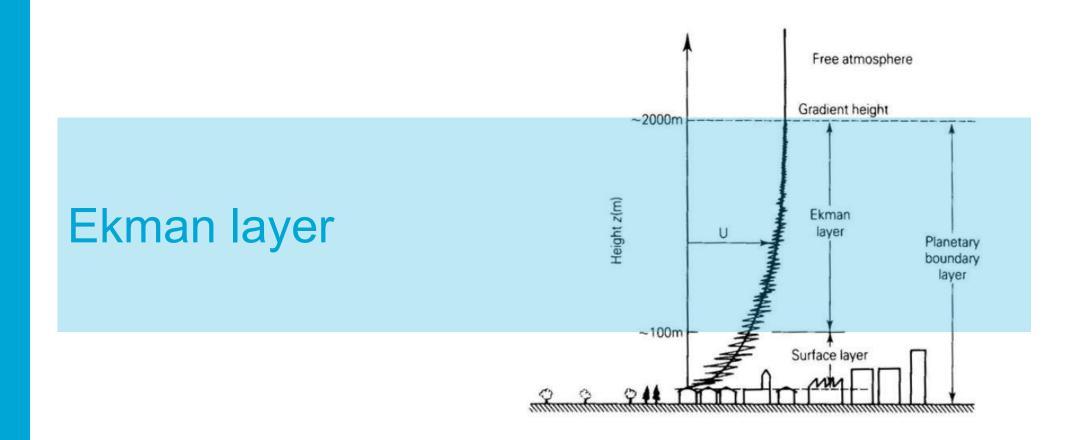
- Wave height
- Fetch
- Wave age



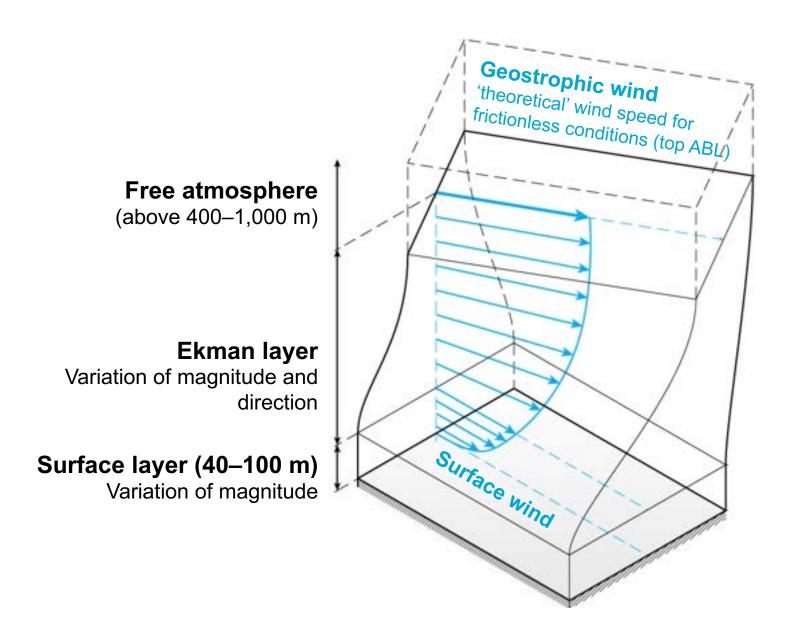
Charnock relation

$$z_{0,\text{Charnock}} = \alpha \frac{u_*^2}{g}$$

Source: Taylor and Yelland (2001)





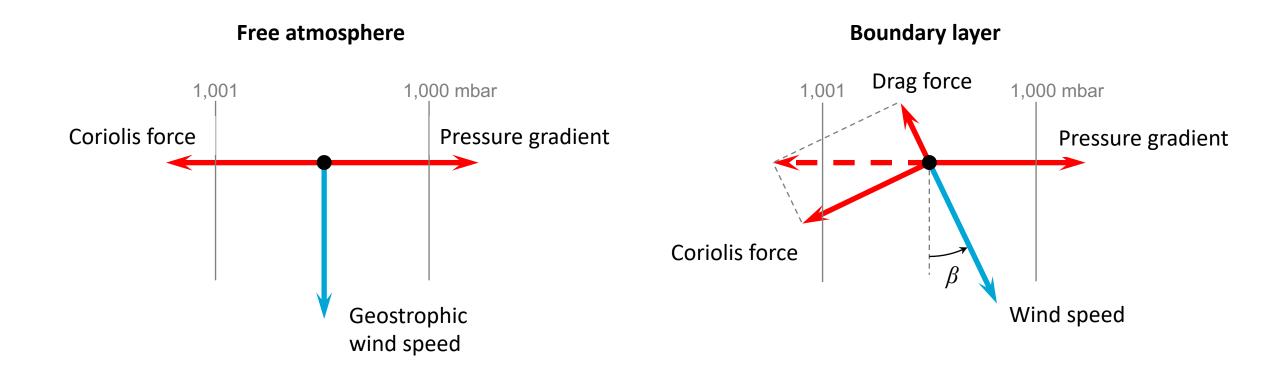


Ekman layer equations

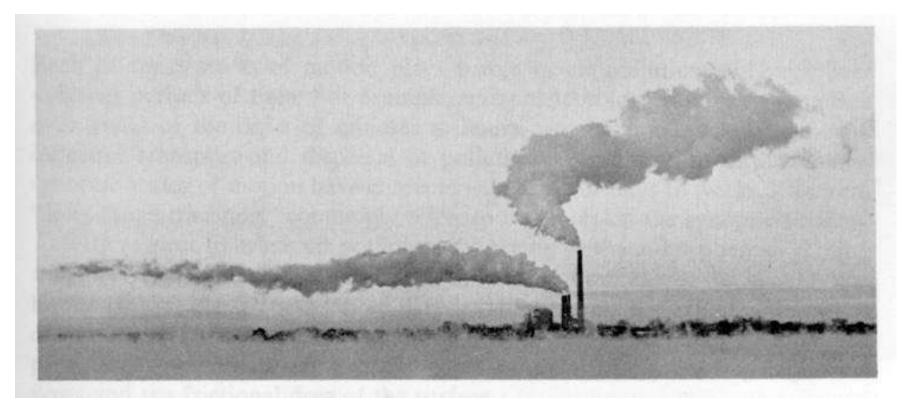
(steady state, horizontally homogeneous)

$$-f_c v + \frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{\partial}{\partial z} \left(\nu_t \frac{\partial u}{\partial z} \right) = 0$$
$$f_c u + \frac{1}{\rho} \frac{\partial p}{\partial y} - \frac{\partial}{\partial z} \left(\nu_t \frac{\partial v}{\partial z} \right) = 0$$

Geostrophic departure in the Ekman layer



ABL Wind field is NOT uni-directional



Stacks in Salem, Massachusetts. Photo by: Ralph Turcotte, Beverly Times

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Geostrophic drag law

also called resistance laws or Rossby number similarity theory

Asymptotic matching of the surface layer and the Ekman layer yields

$$G = \frac{u_*}{\kappa} \sqrt{\left(\ln\left(\frac{u_*}{f_c z_0}\right) - A\right)^2 + B^2}$$

$$\sin \alpha = -\frac{Bu_*}{\kappa G}$$

with

G the magnitude of geostrophic wind speed

lpha the angle between the near-surface winds and the geostrophic wind

A = 1.8 an empirical constant

B = 4.5 an empirical constant

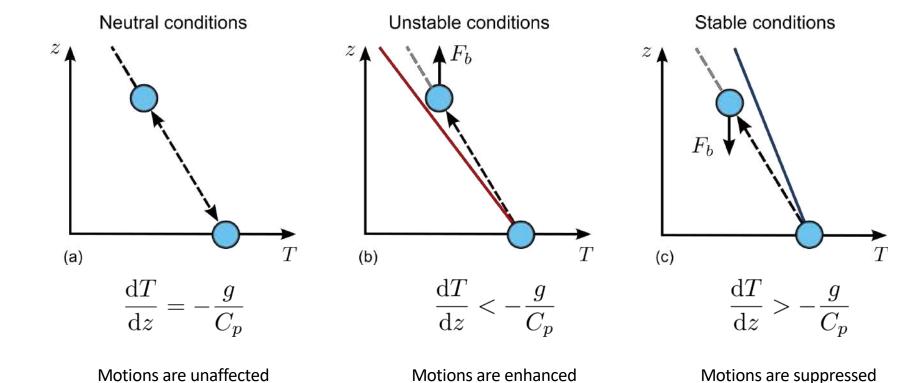
Atmospheric stability



Thermal stability

Adiabatic lapse rate

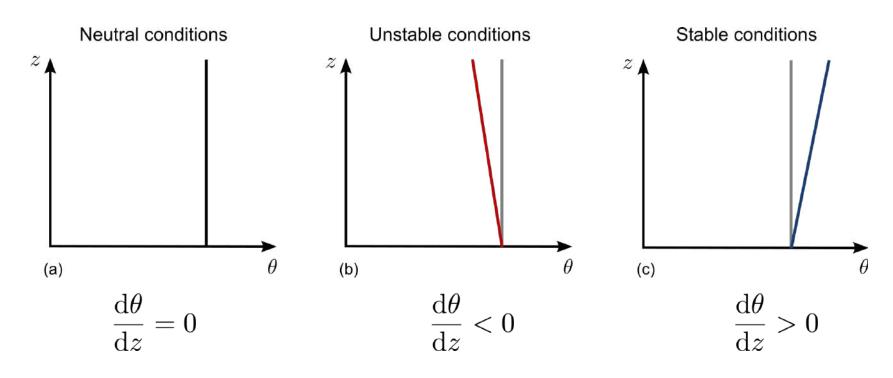
$$\Gamma_d = -\frac{g}{C_p} = -9.8 \text{ K/km}$$



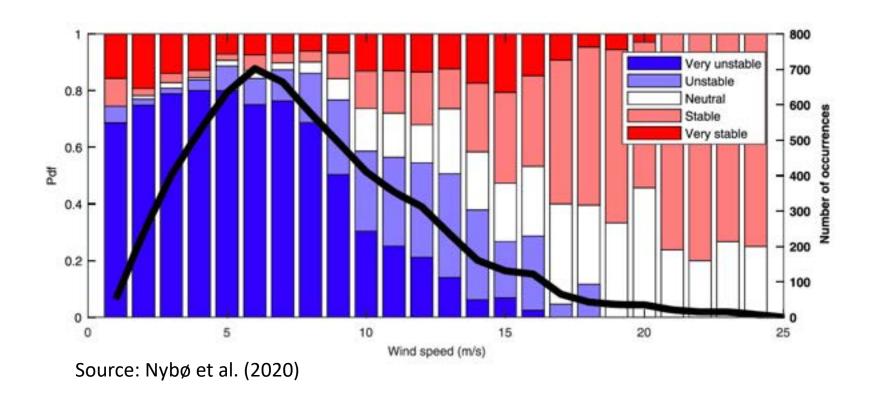
Potential temperature

= temperature an air parcel with pressure p would attain if adiabatically brought to a reference pressure p_0

$$\theta = T \left(\frac{p_0}{p}\right)^{R/C_p}$$



Stable, neutral and unstable conditions



Example: Stability distribution at FINO-1

Stable conditions

- Over land at night (clear skies)
- Warm air advected over cold surface

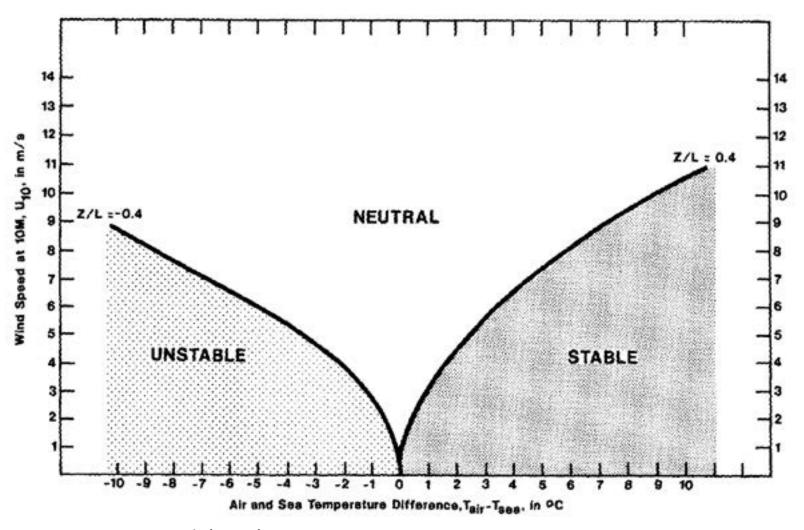
Neutral conditions

- Strong winds & overcast conditions
- Short transition period after sunset

Unstable conditions

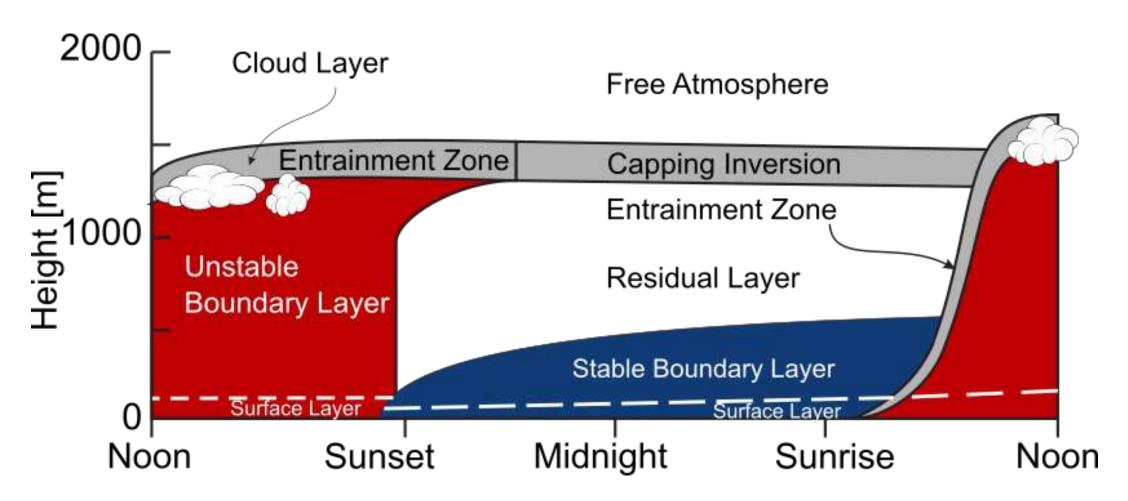
- Over land during daytime
- Cold air advected over warm surface

Atmospheric stability offshore



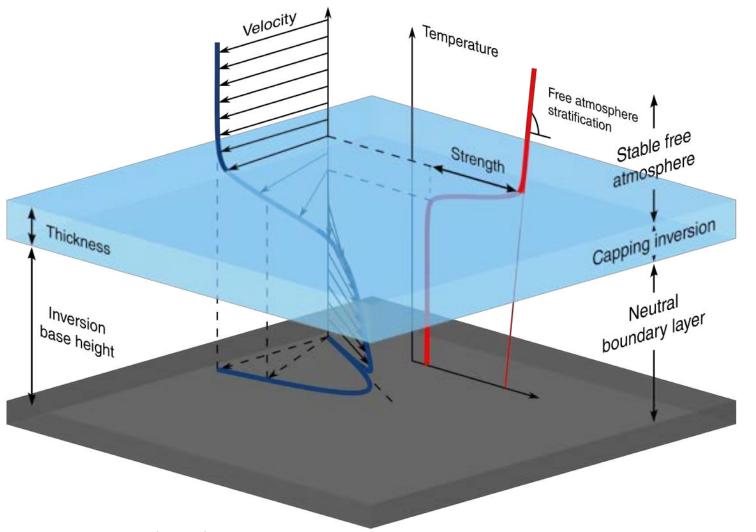
Source: Hsu et al. (1994)

Diurnal cycle



Unstable boundary layer is also called the Convective Boundary Layer (CBL)

Different "types" of stability



Free atmosphere stratification

Always stably stratified

Capping inversion/Inversion layer very stable layer at the top of the ABL

Surface layer stability neutral, stable or unstable

Source: Allaerts (2016)

Atmospheric stability metrics: Obukhov length

$$L = -\frac{u_*^3}{\kappa g \alpha \overline{w' \theta'}}$$

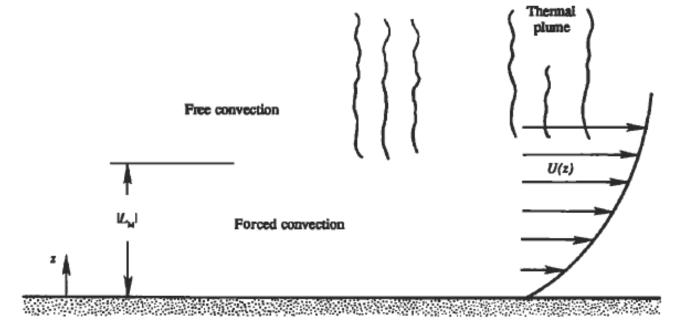
with u_* friction velocity $\overline{w'\theta'}$ kinematic heat flux κ von Karman constant g gravitational acceleration α thermal expansion coefficient cfr. $\rho = \rho_0[1 - \alpha(T - T_0)]$

Interpretation:

$$\frac{z}{L} = \zeta \sim \frac{\text{buoyant destruction}}{\text{shear production}}$$

 $z \ll |L|$: shear production dominates (mechanical turbulence)

 $z \gg |L|$: buoyant destruction/production dominates



Source: Kundu et al. (2002)

Atmospheric stability metrics: Richardson number

gradient Richardson number

$$Ri = \frac{\frac{g}{\theta_0} \frac{\partial \theta}{\partial z}}{\left(\frac{\partial u}{\partial z}\right)^2 + \left(\frac{\partial v}{\partial z}\right)^2}$$

flux Richardson number

$$R_f = \frac{\frac{g}{\theta_0} \overline{w'\theta'}}{\overline{u_i' u_j'} \frac{\partial \overline{u_i}}{\partial x_j}}$$



bulk Richardson number

$$R_B = \frac{\frac{g}{\theta_0} \Delta \theta \Delta z}{\left(\Delta u\right)^2 + \left(\Delta v\right)^2}$$

Empirical relation between Ri and L:

- unstable conditions: $\frac{z}{L} = Ri$
- stable conditions: $\frac{z}{L} = \frac{Ri}{1 5Ri}$

Monin-Obukhov similarity theory

Velocity gradient in the surface layer depends on stability

$$\frac{\kappa z}{u_*} \frac{dU}{dz} = \Phi(\zeta)$$

Universal function from experimental data

$$\zeta > 0$$
: $\Phi(\zeta) = 1 + \beta \zeta$
 $\zeta < 0$: $\Phi(\zeta) = (1 - \gamma \zeta)^{-1/4}$

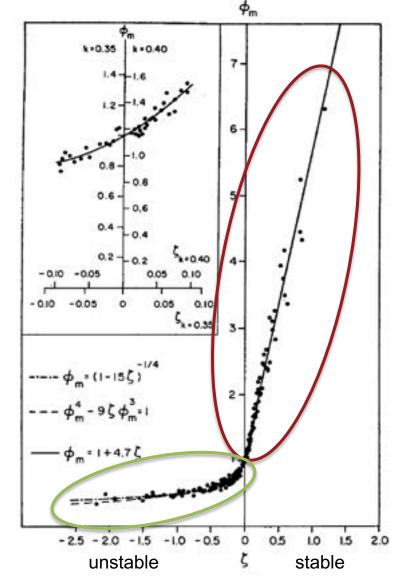
with empirical constant $\beta \approx 4.7$, $\gamma \approx 15$

Integration leads to an expression for the wind profile:

$$\to U(z) = \frac{u_*}{\kappa} \left[\ln \left(\frac{z}{z_0} \right) - \Psi \left(\frac{z}{L} \right) + \Psi \left(\frac{z_0}{L} \right) \right]$$

where

$$\Psi(\zeta) = \int_{\zeta_0}^{\zeta} \frac{1 - \Phi(x)}{x} dx$$



Source: Businger et al. (1971)

Monin-Obukhov similarity theory

$$U(z) = \frac{u_*}{\kappa} \left[\ln \left(\frac{z}{z_0} \right) - \Psi \left(\frac{z}{L} \right) + \Psi \left(\frac{z_0}{L} \right) \right]$$

with stability correction functions

$$\zeta = 0$$
: $\Psi(\zeta) = 0$

$$\zeta > 0$$
: $\Psi(\zeta) = -\beta \zeta$

$$\zeta < 0$$
: $\Psi(\zeta) = 2 \ln\left(\frac{1+x}{2}\right) + \ln\left(\frac{1+x^2}{2}\right) - 2 \tan^{-1} x + \frac{\pi}{2}$, $x = (1-\gamma\zeta)^{-1/4}$

with empirical constant $\beta \approx 4.7$, $\gamma \approx 15$

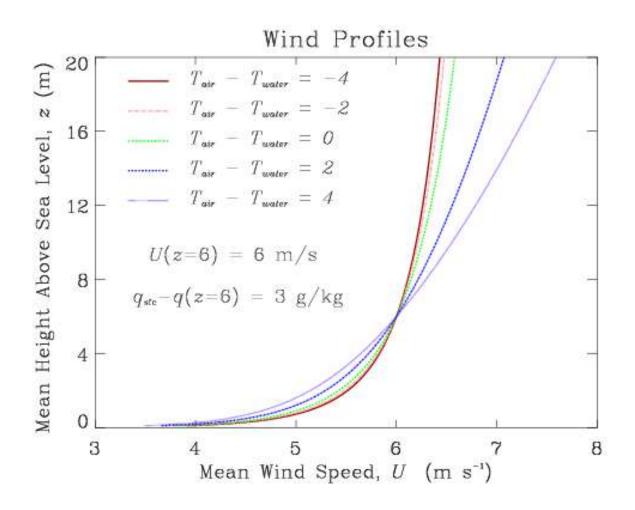
Similar expressions can be found for the temperature

$$\zeta=0$$
: $\Phi(\zeta)=1$
 $\zeta>0$: $\Phi(\zeta)=1+\beta\zeta$
 $\zeta<0$: $\Phi(\zeta)=(1-\gamma\zeta)^{-1/4}$
and

$$\Psi(\zeta) = \int_{\zeta_0}^{\zeta} \frac{1 - \Phi(x)}{x} dx$$

$$x=(1-\gamma\zeta)^{-1/4}$$

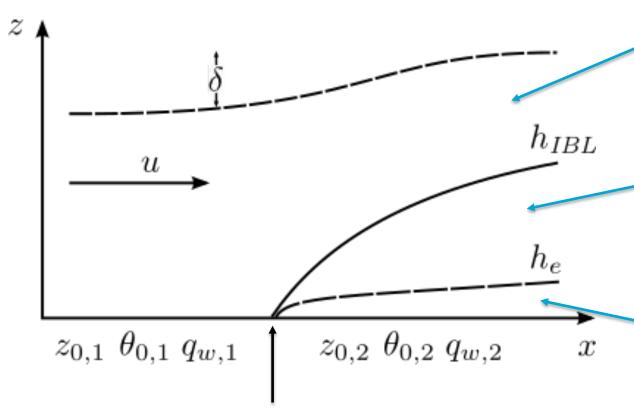
Influence of thermal effects on wind shear



Selected topics of interest



Internal boundary layer (IBL) theory



Discontinuity in surface conditions, e.g., land-sea transition

Free stream: Flow is characteristic of the upstream conditions (except for a displacement δ of the outer flow field)

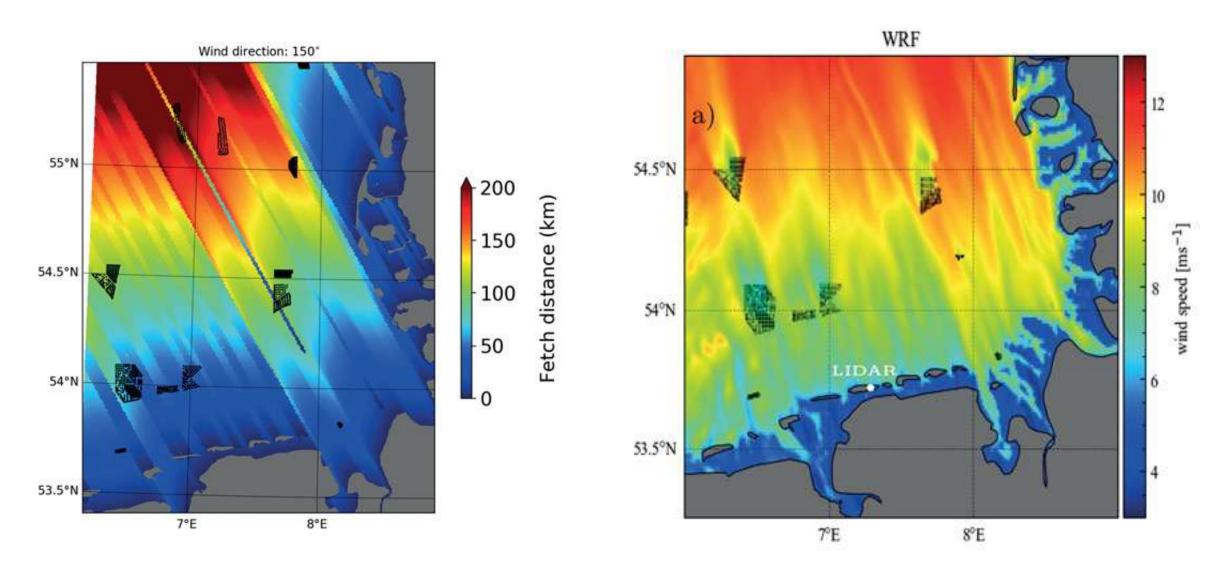
Internal boundary layer: Region where the velocity and turbulent stress are significantly affected by the change in surface conditions

Equilibrium layer: Wind profile has completely adjusted to the local surface conditions

$$\frac{h_{ibl}(x)}{z_{0,2}} \sim \left(\frac{x}{z_{0,2}}\right)^{0.8}$$

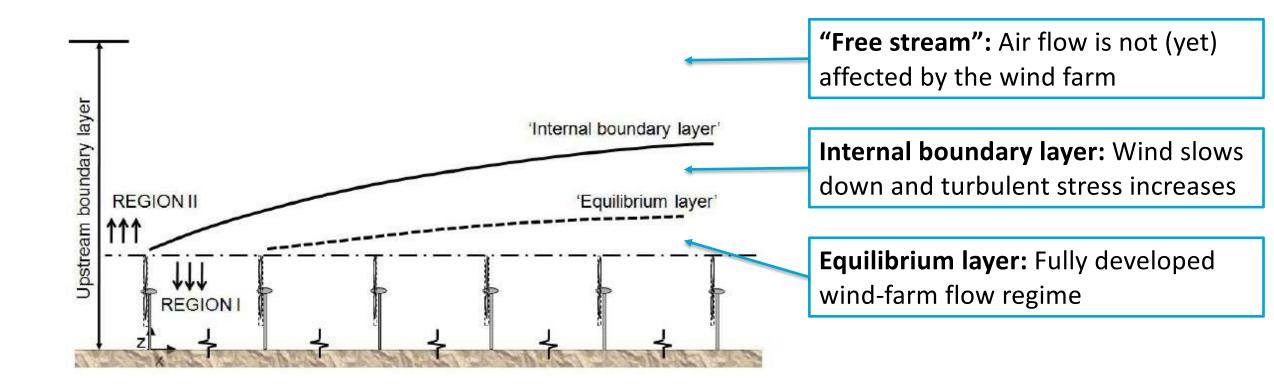
Source: Garratt (1990)

IBL example: Coastal effects



Source: Schulz-StellenFleth et al. (2022)

Wind-farm internal boundary layer

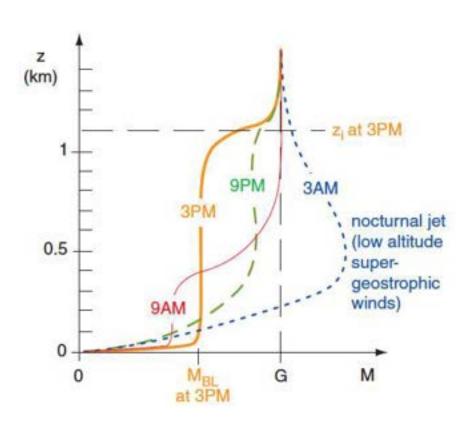


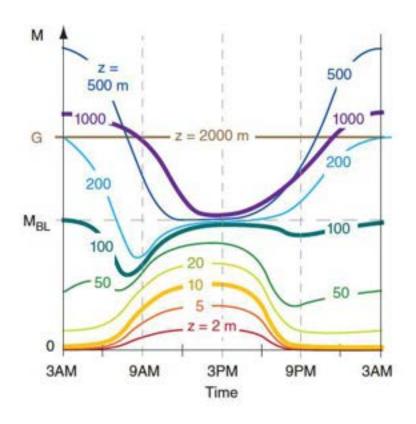
From a large-scale perspective, a wind farm can be treated as a special case of roughness transition.

Source: Chamorro and Porté-Agel (2011)

Low-level jet

= supergeostrophic wind speed at low altitudes, occurs often at night over land





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Source: Stull (2016)

Low-level jet

The Blackadar (1957) model

Starting from dynamic Ekman layer equations

$$\frac{\partial U}{\partial t} = f_c V + \frac{\partial \tau_{zz}}{\partial z}$$

$$\frac{\partial V}{\partial t} = f_c(G - U) + \frac{\partial \tau_{yz}}{\partial z}$$

Friction disappears at sunset

$$\frac{\partial^2 U}{\partial t^2} = f_c^2 (G - U)$$

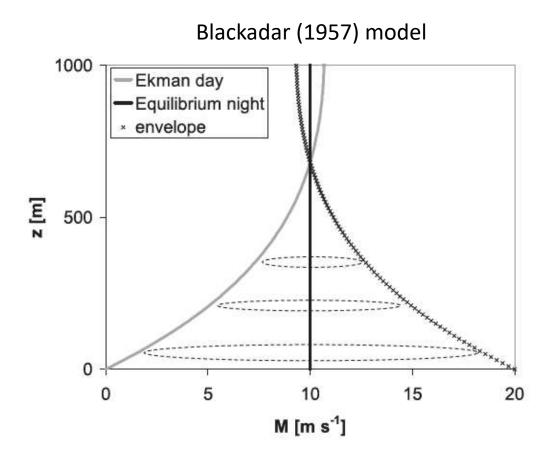
$$U = G + V_0 \sin(f_c t) + (U_0 - G)\cos(f_c t)$$

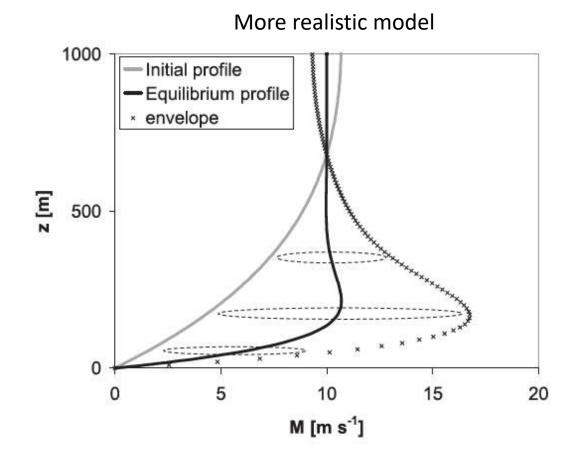
$$V = V_0 \cos(f_c t) - (U_0 - G)\sin(f_c t)$$

Undamped inertial oscillation about the geostrophic wind with period $2\pi/f_c$

e.g. $f_c = 10^{-4} s^{-1}$ yields an inertial period of about 17h

Low-level jet





Source: van de Wiel et al. (2010)

Flow over a hill

Flow regimes:

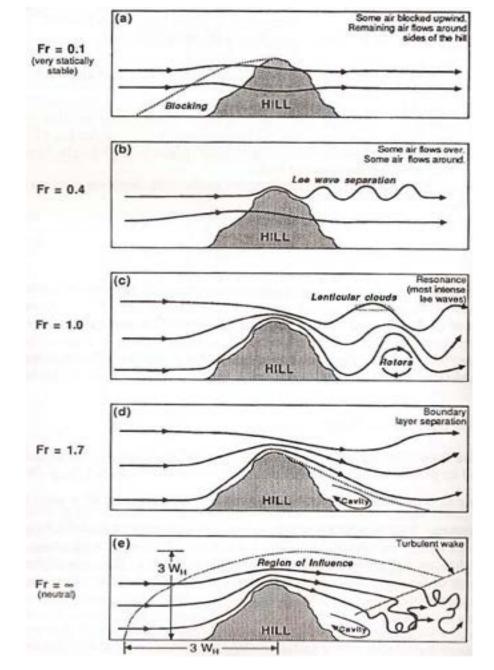
- Fr<< 1, blockage upstream, flow goes round rather than above mountain
- Fr ~ 1, wave resonance above ridge, strong downslope winds, and turbulent rotors in the lee
- Fr >> 1, neutral flow, little blockage, flow goes above ridge, separated cavity type flow in the lee

Froude number

$$Fr = rac{U}{N \, W}$$

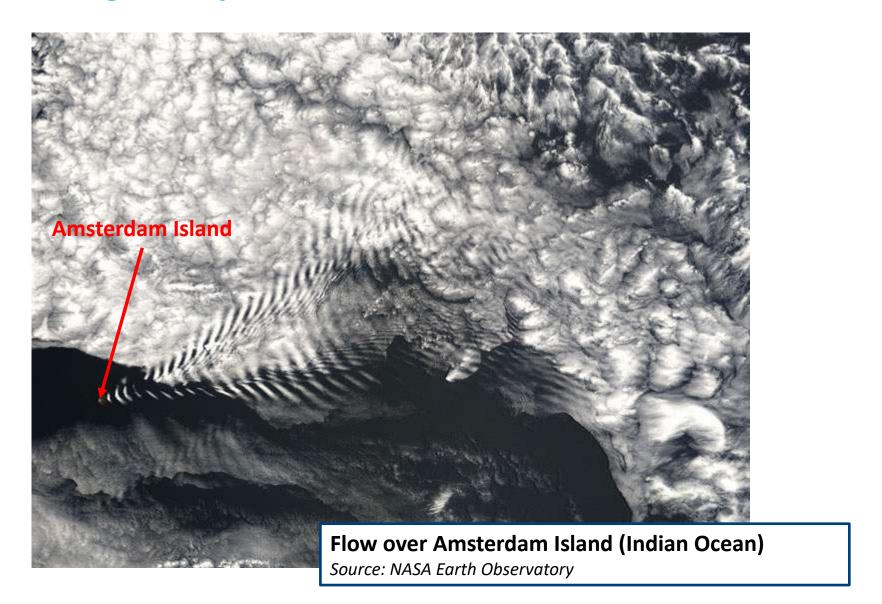
Brunt Väisälä frequency

$$N = \sqrt{rac{g}{ heta_0} rac{\partial heta}{\partial z}}$$

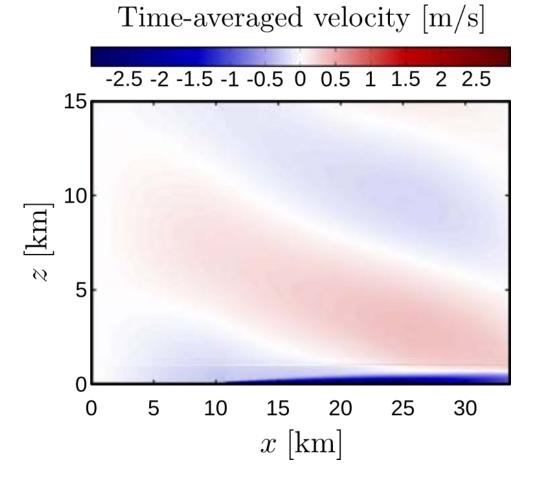


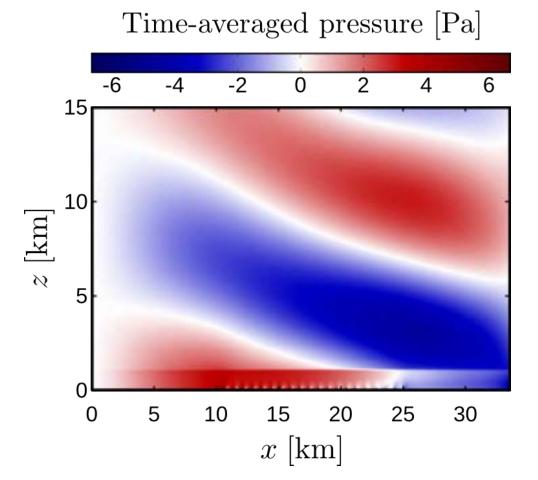
Source: Stull (1988)

Atmospheric gravity waves



Wind-farm-induced atmospheric gravity waves





Source: Allaerts (2016)

Outline

Motivation and objectives

Overview of relevant reference material

General meteorology

Boundary-layer meteorology

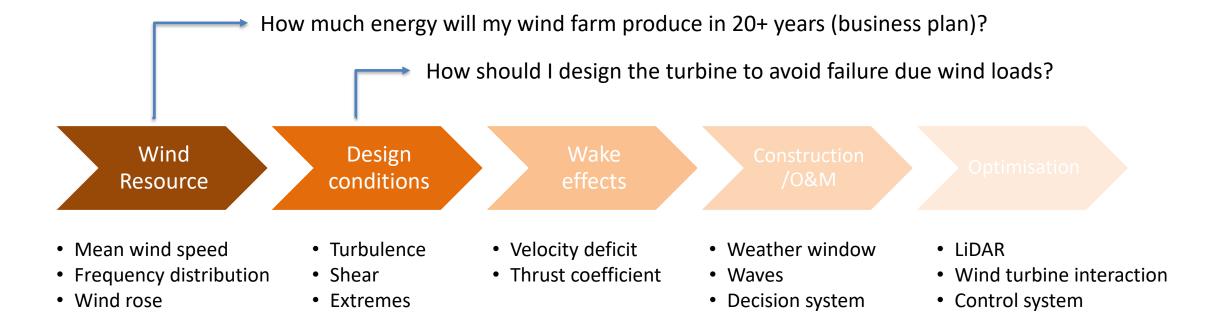
"The physics-based approach"

Part 3: Wind power meteorology "The engineering/statistical/industry approach"

Take-home messages

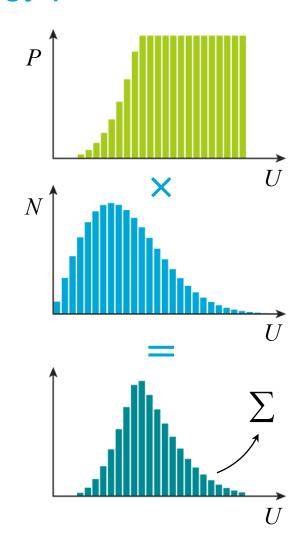


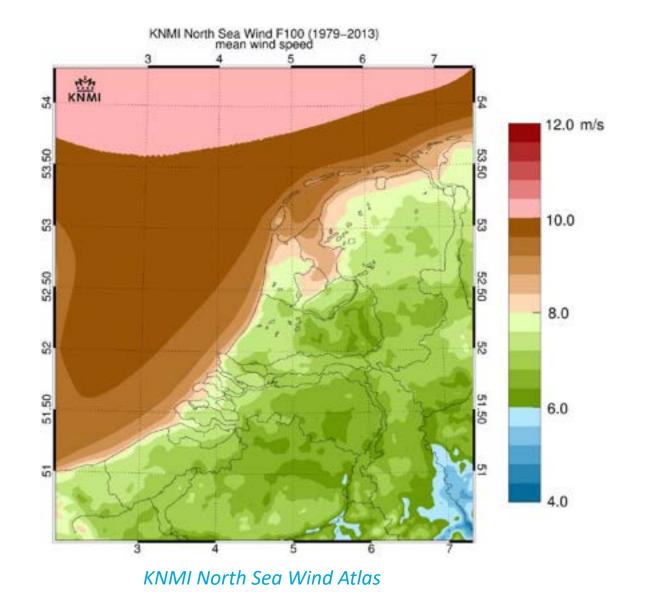
The importance of meteorological aspects



Why wind power meteorology?

Energy production





Why wind power meteorology?

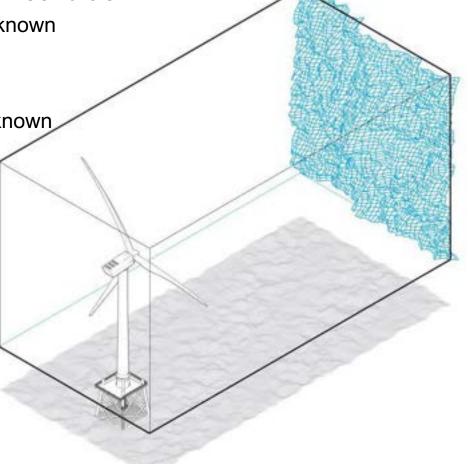
Design

Generate turbulent wind field / random sea for given condition

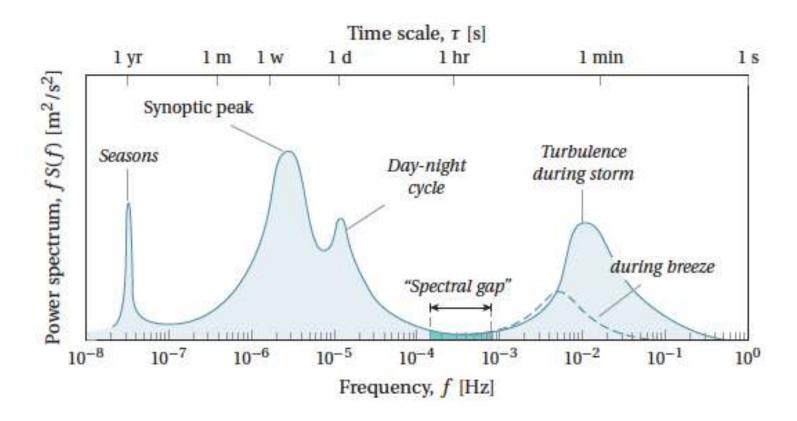
Short-term characteristics of wind and waves have to be known

How often does a certain condition occur?

Long-term characteristics of wind and waves have to be known



Temporal variability of wind



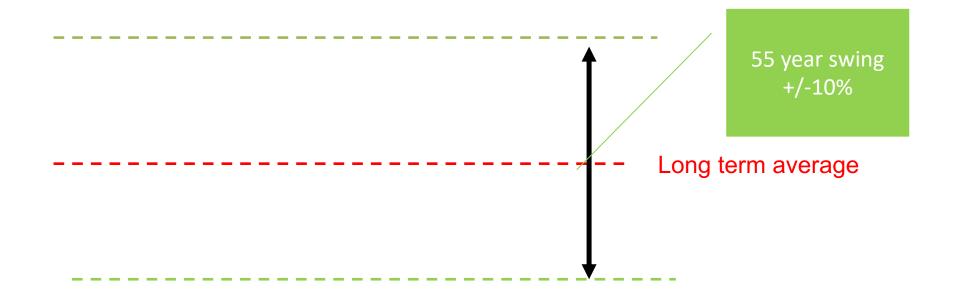
Categories of wind speed variations:

- Inter-annual
- Annual (seasonal/monthly)
- Diurnal
- Short term (gusts and turbulence)

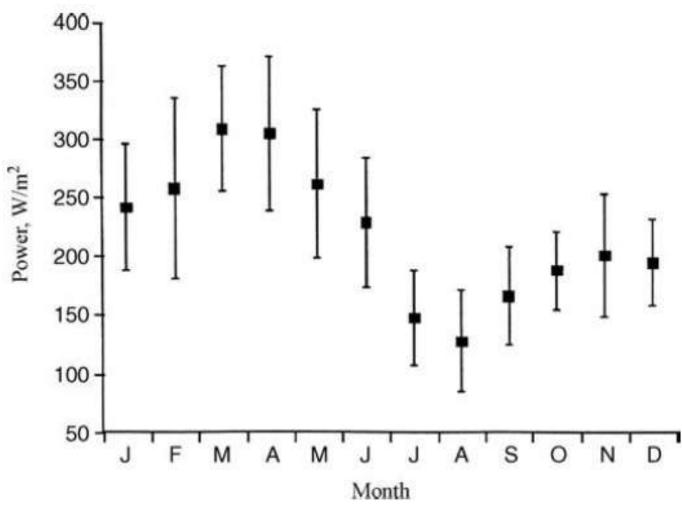
van der Hoven spectrum (1957)

Figure source: Bos (2017)

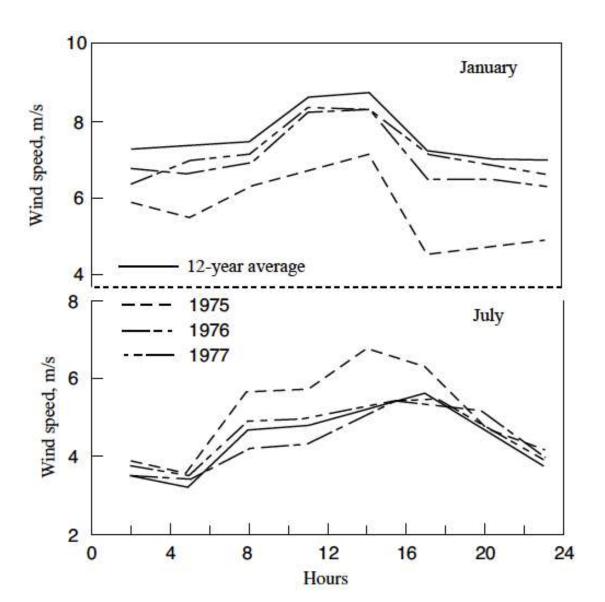
Inter-annual variability (UK Example)



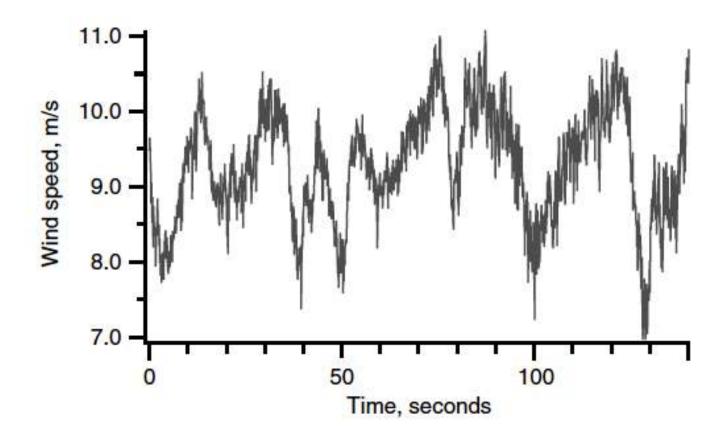
Annual variability (Amarillo, Texas)



Diurnal variability (Casper, Wyoming)



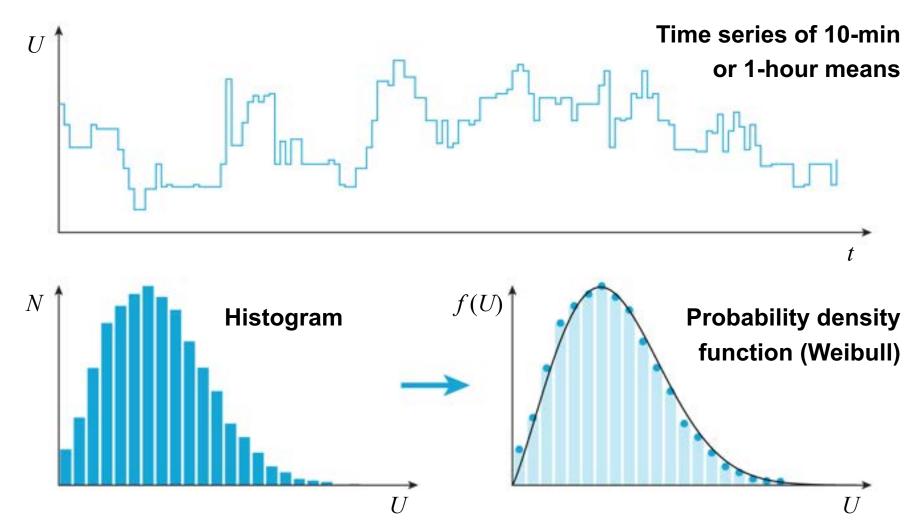
Short-term variability



Source: Manwell et al. (2009)

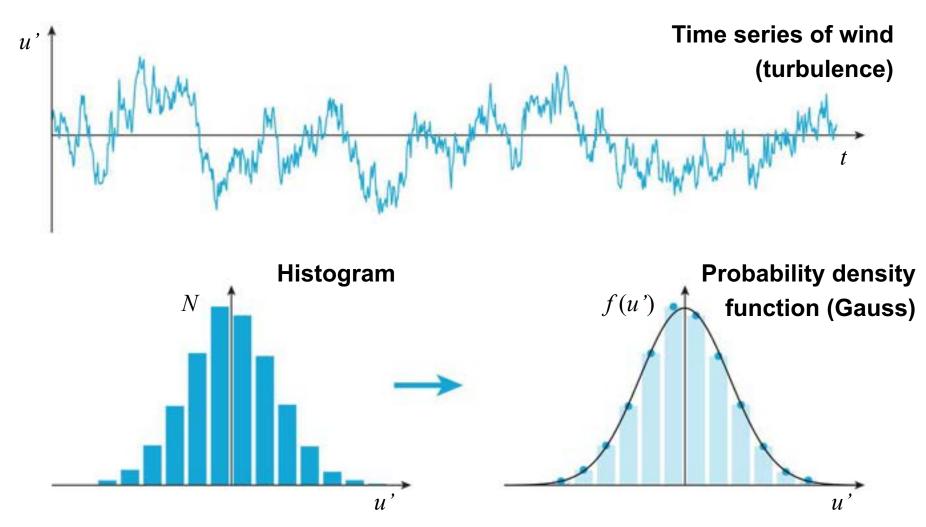
Basic wind statistics

Long-term variability



Basic wind statistics

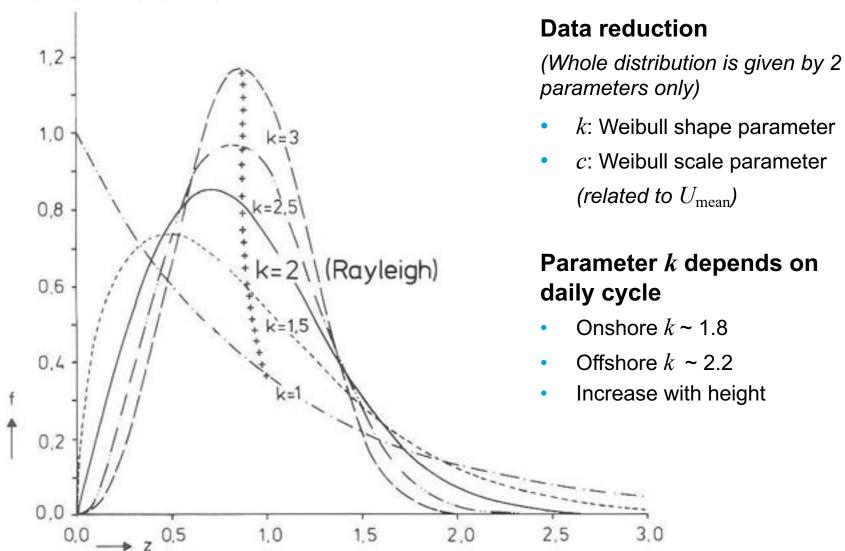
Short-term variability



Long-term wind statistics for wind resource assessment

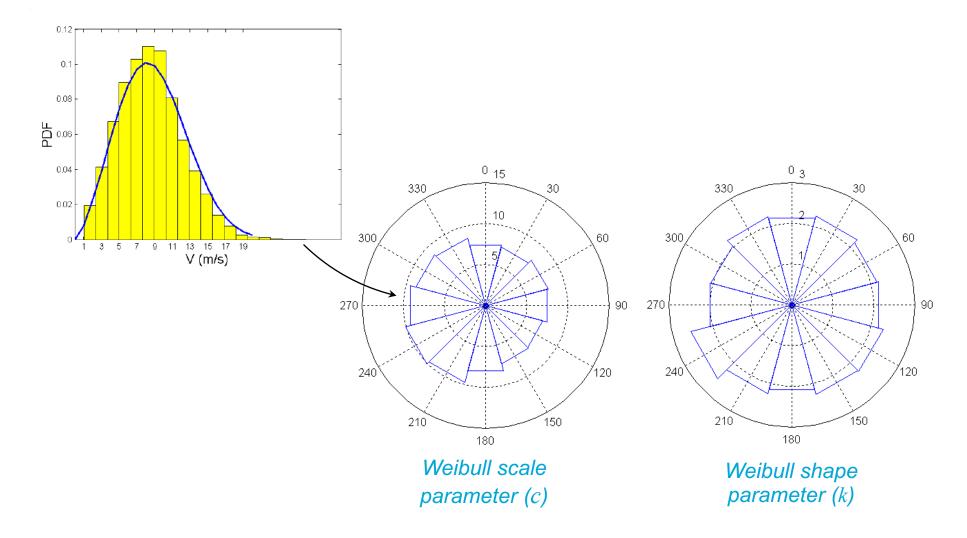


Weibull distribution



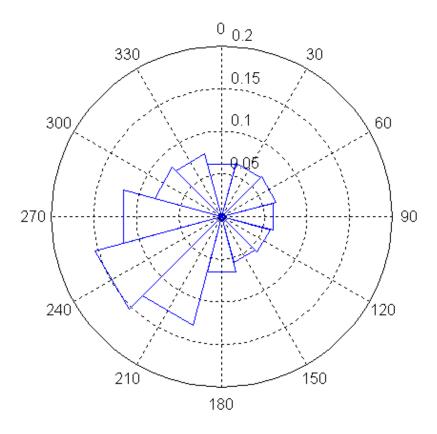
Weibull distribution

- Fit for each wind direction sector



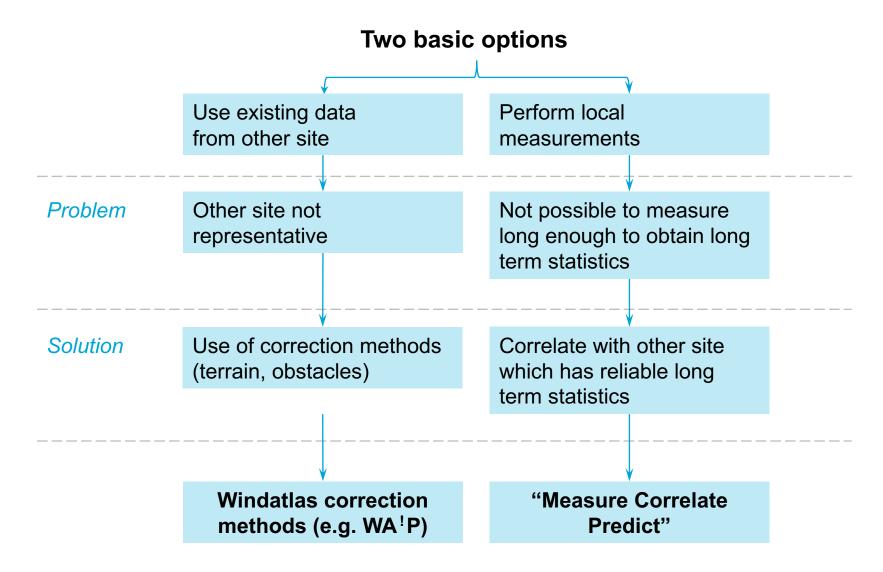
Weibull distribution

- Wind rose

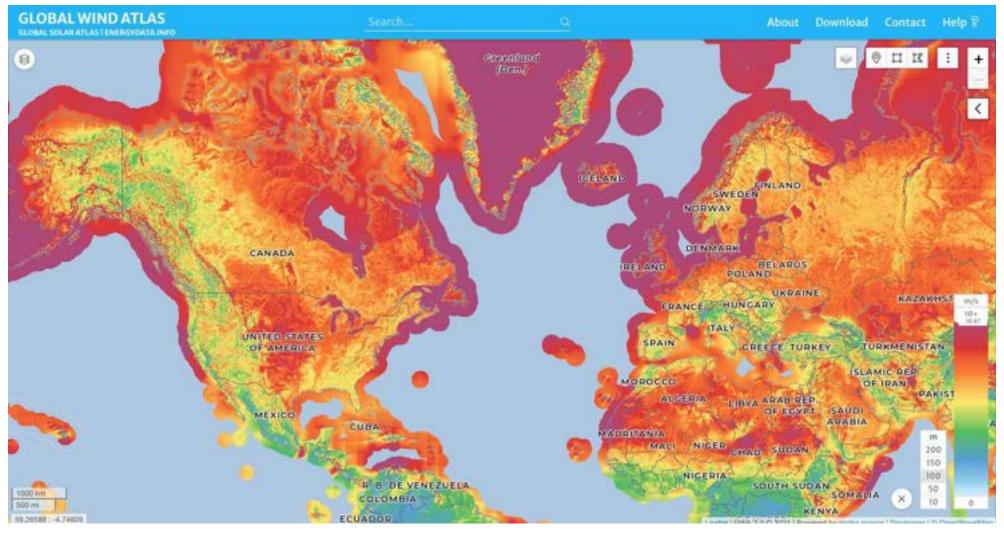


Frequency of occurrences

How to obtain wind statistics for a given location?

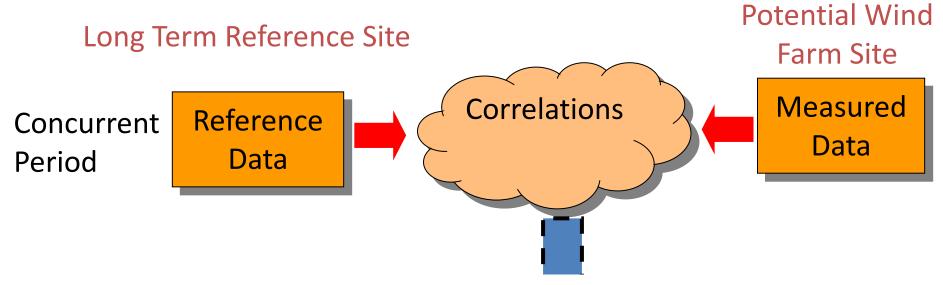


Long term wind statistics: Wind atlas

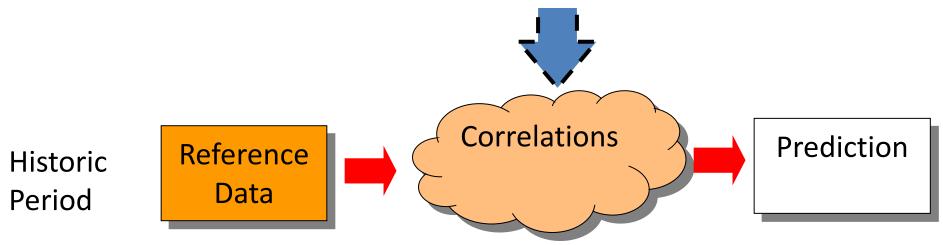


Source: https://globalwindatlas.info/

Measure-Correlate-Predict



Assumes wind climate will not change over lifetime of wind farm!



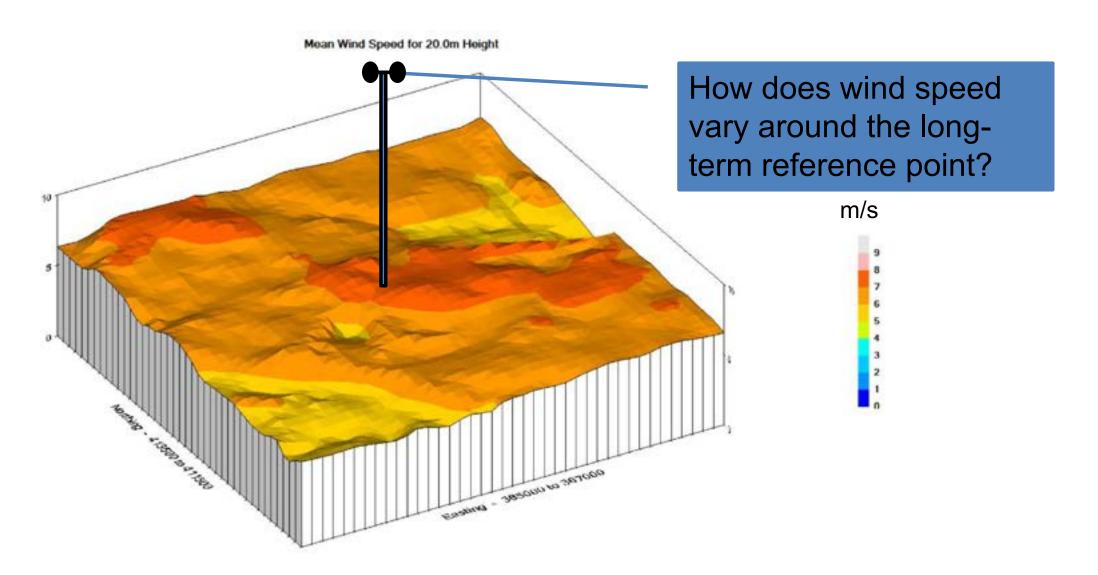
Reanalysis projects

By (inter)national centers: NCEP/NCAR, ECMWF

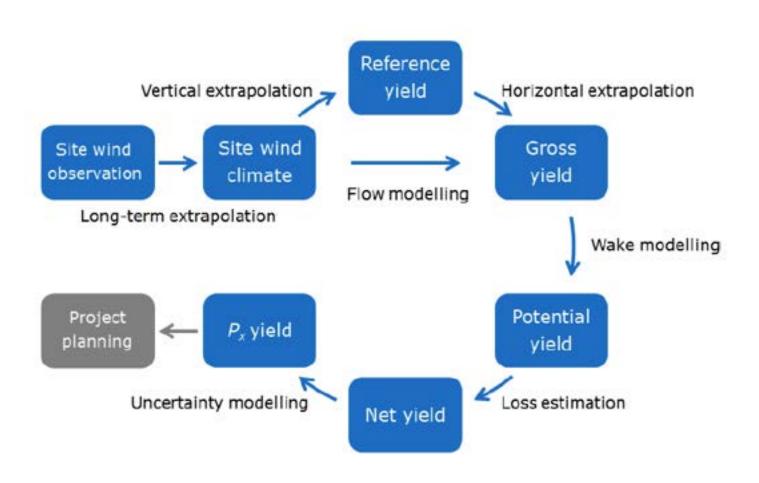
- Collection of all kind of data (*weather stations, radiosondes, aircraft, ships, buoys,*); not restricted to routine weather forecast
- One (state-of-the-art) method; avoid apparant jumps in weather due to other NWP model

- Homogeneous data sets covering a long period (from 1899!) and global scale;
 suitable for climate studies
- Resolution 2.5° to 5° (100–200 km); 6 or 12 hourly
- Can provide initial and boundary conditions meso scale models
- MERRA, ERA Interim,

We Have a Long Term Wind Distribution: Now What?



Steps in wind resource and energy yield assessment procedure



Vertical extrapolation

- Logarithmic profile
- Power law
- More sophisticated?

Horizontal extrapolation

- Mass-consistent models
- Linearised models
- CFD models

Source: Mortensen et al. (2015)



Questions?



Take-home messages

- Atmospheric science is fun and very relevant to wind energy
- The wind resource is a complex phenomenon covering a wide range of temporal and spatial scales
- There is more to the atmospheric boundary layer than just the logarithmic wind profile and the Weibull distribution
- If you want to learn more, read one of the books under reference material



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